

Prehľad vzorcov integrálneho počtu

| Funkcia $f : y = f(x)$ | Vzorec pre neurčitý integrál $\int f(x)dx = F(x) + c$ | Podmienky platnosti vzorca $(x \in D(f))$ |
|--|---|--|
| $y = 0$ | $\int 0 dx = c (c \in R)$ | $x \in (-\infty; +\infty)$ |
| $y = 1$ | $\int dx = x + c$ | $x \in (-\infty; +\infty)$ |
| $y = x^n, n \in \mathbb{N}$ | $\int x^n dx = \frac{x^{n+1}}{n+1} + c$ | $x \in (-\infty; +\infty)$ |
| $y = \frac{1}{x}$ | $\int \frac{1}{x} dx = \ln x + c$ | $x \in (-\infty; 0) \cup (0; \infty)$ |
| $y = e^x$ | $\int e^x dx = e^x + c$ | $x \in (-\infty; +\infty)$ |
| $y = a^x (a > 0, a \neq 1)$ | $\int a^x dx = \frac{a^x}{\ln a} + c$ | $x \in (-\infty; +\infty)$ |
| $y = \sin x$ | $\int \sin x dx = -\cos x + c$ | $x \in (-\infty; +\infty)$ |
| $y = \cos x$ | $\int \cos x dx = \sin x + c$ | $x \in (-\infty; +\infty)$ |
| $y = \operatorname{tg} x$ | $\int \operatorname{tg} x dx = -\ln \cos x + c$ | $\cos x \neq 0, x \neq \frac{\pi}{2} + k\pi, k \text{ celé}$ |
| $y = \operatorname{cotg} x$ | $\int \operatorname{cotg} x dx = \ln \sin x + c$ | $\sin x \neq 0, x \neq k\pi, k \text{ celé}$ |
| $y = \frac{1}{\cos^2 x}$ | $\int \frac{1}{\cos^2 x} dx = \operatorname{tg} x + c$ | $x \in \bigcup_{k \in \mathbb{Z}} \left((2k-1)\frac{\pi}{2}; (2k+1)\frac{\pi}{2} \right)$ |
| $y = \frac{1}{\sin^2 x}$ | $\int \frac{1}{\sin^2 x} dx = -\operatorname{cotg} x + c$ | $x \in \bigcup_{k \in \mathbb{Z}} (k\pi, (k+1)\pi)$ |
| $y = \frac{1}{\sqrt{1-x^2}}$ | $\int \frac{1}{\sqrt{1-x^2}} dx = \arccos x + c$ | $x \in (-1, 1)$ |
| $y = -\frac{1}{\sqrt{1-x^2}}$ | $\int -\frac{1}{\sqrt{1-x^2}} dx = \arcsin x + c$ | $x \in (-1, 1)$ |
| $y = \frac{1}{1+x^2}$ | $\int \frac{1}{1+x^2} dx = \operatorname{arctg} x + c$ | $x \in (-\infty; +\infty)$ |
| $y = -\frac{1}{1+x^2}$ | $\int -\frac{1}{1+x^2} dx = \operatorname{arcctg} x + c$ | $x \in (-\infty; +\infty)$ |
| $\int af(x)dx = a \int f(x)dx$ $\int \frac{f'(x)}{f(x)} dx = \ln f(x) + c$ $\int [f(x) \pm g(x)]dx = \int f(x)dx \pm \int g(x)dx$ $\int f(x)dx = \int f[\varphi(t)]\varphi'(t)dt + c$ $\int u'v dx = uv - \int uv' dx$ $\int \frac{1}{x^2 + px + q} dx = \frac{1}{\sqrt{q - \left(\frac{p}{2}\right)^2}} \operatorname{atrc tg} \frac{x + \frac{p}{2}}{\sqrt{q - \left(\frac{p}{2}\right)^2}} + c$ | | |